

বাস্তব সংখ্যা (Poll Time)

নিচের সংখ্যা গুলো এর মধ্যে মূলদ সংখ্যা বের কর -

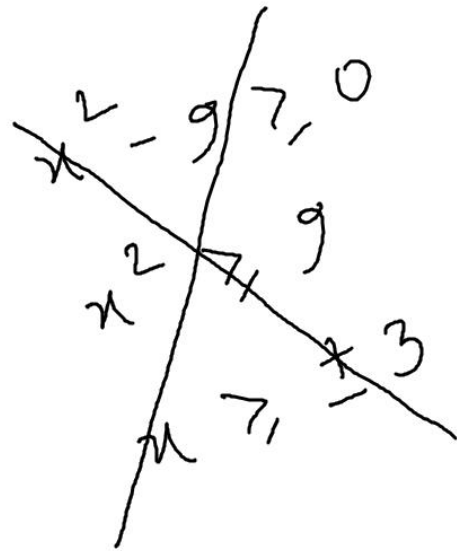
- i. 2.5 ✓
- ii. 3.1416.... ✗
- iii. $\frac{22}{7}$ ✓
- iv. 111.1111..... ✓
- v. 2020 ✓
- vi. 2.058 ✓
- vii. e^2 ✗
- viii. infinity ✗

Options:

- A. i, iii, iv, v, vi, vii
- B. i, iii, iv, v, vi, viii
- C. i, iii, iv, v, vi
- D. i, iii, iv, v, vii, viii



অসমতা



$$x^2 - 9 \geq 0$$
$$(x+3)(x-3) \geq 0$$



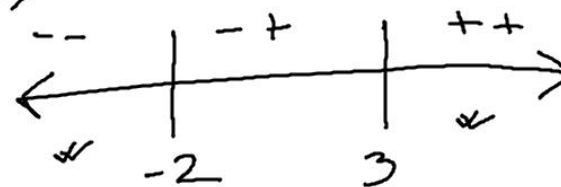
$$x \leq -3 \text{ or } x \geq 3$$



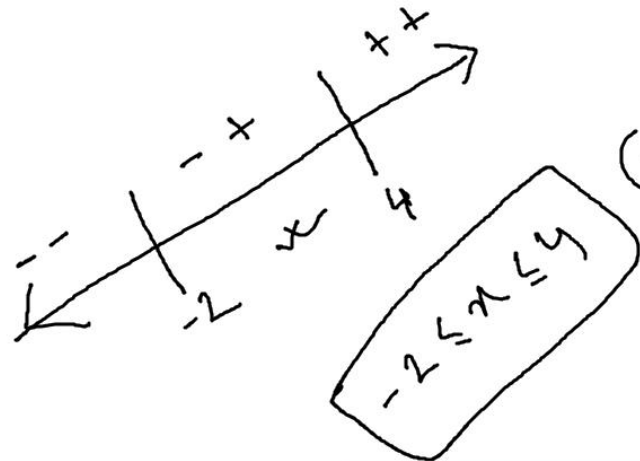
অসমতা

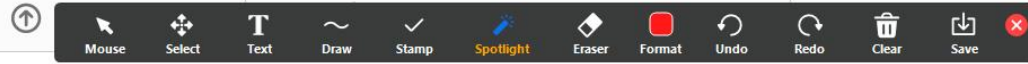
$$x^2 - x - 6 \geq 0$$
$$(x-3)(x+2) \geq 0$$

$$x \leq -2 \text{ or } x > 3$$



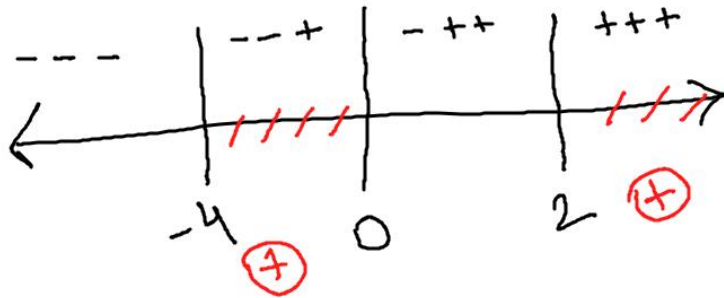
$$x^2 - 2x - 8 \leq 0$$
$$(x-4)(x+2) \leq 0$$





অসমতা ✓

$$x(x-2)(x+4) \geq 0$$



$-4 \leq x \leq 0$ OR $x > 2$

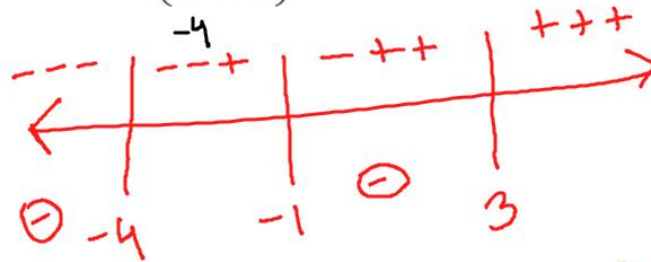


অসমতা (Poll Time – NDC previous Year)

$$\frac{(x - 3)(x + 1)}{(x + 4)} \leq 0$$

Option:

- A. $x \leq -4$ or $-1 \leq x \leq 3$
- B. $x < -4$ or $-1 \leq x \leq 3$ ✓
- C. $x < -4$ or $-1 < x < 3$
- D. $x \leq -4$ or $-1 < x \leq 3$



$$x \leq -4$$

$$\text{or } x < -4$$

$$\text{or } -1 \leq x \leq 3$$



উদ্ভাস
Since 2000

ফাংশন

$y = f(x)$ মানে কি?

• $2x + 3y = 10$

• $x^2 + y^2 = 9$

• $x^2 = y$

• $x = y^2$

• $y = 10$

$x = f(y)$

$x = 1$

$2 \cdot 1 + 3y = 10$

$y = 8/3$

$y = f(x)$

$x = 1$

$x^2 + y^2 = 9$

$y^2 = 8$

$y = \pm\sqrt{8}$

$x = 2$
 $y = 4$

$x = 1$
 $y^2 = 1$
 $y = \pm 1$

$y \neq f(x)$

$x = 5$ $y = 10$
Constant

$x = -2$
 $y = 10$



ফাংশন Domain

- Case 1: $\frac{c}{\square}$
- Case 2: $\sqrt[c]{\square}$ $D_f = \mathbb{R}$
- Case 3: Special Function (e.g. sin, cos, log, ln ... etc.)

$$f(x) = \frac{x^2 + 10}{\square}$$

$$D_f = \mathbb{R}$$

$$f(x) = \frac{x^{100} + x^{99} + \dots + 1}{\square}$$

$$D_f = \mathbb{R}$$

$$f(x) = \frac{|x + 3|}{\square}$$

$$D_f = \mathbb{R}$$



ফাংশন Domain (Case 1)

- Case 1 : $\frac{c}{x}$;

Domain নির্ণয় কর:

- $f(x) = \frac{5x}{3x-2}$

- $f(x) = \frac{x}{x^2-3x-4}$

- $f(x) = \frac{x^2}{x^2+1}$ [NDC Previous year]

- $f(x) = \frac{x^2-1}{x+1}$ [NDC Previous year]

$3x-2 \neq 0$
 $x \neq \frac{2}{3}$

$D_f = \mathbb{R} - \left\{ \frac{2}{3} \right\}$

$x^2-3x-4 \neq 0$
 $(x-4)(x+1) \neq 0$

$D_f = \mathbb{R} - \{4, -1\}$

$x \neq 4, -1$

$D_f = \mathbb{R} - \{ \}$

$x^2+1 \neq 0$
 $x^2 \neq -1$
 $x \neq \sqrt{-1}$



ফাংশন Domain (Case 1)

- Case 1 : $\frac{c}{a}$; $a \neq 0$

Domain নির্ণয় কর:

- $f(x) = \frac{5x}{3x-2}$
- $f(x) = \frac{x}{x^2-3x-4}$
- $f(x) = \frac{x^2}{x^2+1}$ [NDC Previous year]
- $f(x) = \frac{x^2-1}{x+1}$ [NDC Previous year]

$$f(x) = \frac{(x+1)(x-1)}{x+1} = x-1$$

$$D_f = \mathbb{R}$$

$$x+1 \neq 0$$

$$x \neq -1$$

$$D_f = \mathbb{R} - \{-1\}$$



ফাংশন Domain (Case 2)

Domain নির্ণয় কর:

- $f(x) = \sqrt[3]{2x-5}$
- $f(x) = \sqrt{x^2+x-5}$
- $f(x) = \sqrt{2x-5}$
- $f(x) = \sqrt[4]{x^2-4}$
- $f(x) = \sqrt[4]{6-x-x^2}$

$D_f = \mathbb{R}$

$D_f = \mathbb{R}$

$2x-5 \geq 0$
 $x \geq 5/2$

$x^2-4 \geq 0$
 $(x+2)(x-2) \geq 0$

$6-x-x^2 \geq 0$
 $x^2+x-6 \leq 0$
 $(x+3)(x-2) \leq 0$



ফাংশন Domain (Case 2) – Complete Overview

Domain নির্ণয় করঃ

• $f(x) = \sqrt[3]{2x+5}$

• $f(x) = \frac{1}{\sqrt[3]{2x+5}}$

• $f(x) = \sqrt[4]{2x+5}$

• $f(x) = \frac{1}{\sqrt[4]{2x+5}}$

$D_f = \mathbb{R}$

$2x+5 \neq 0$
 $x \neq -5/2$

$D_f = \mathbb{R} - \{-5/2\}$

$2x+5 > 0$
 $x > -5/2$

$[-5/2, \infty[$

$2x+5 > 0$
 $x > -5/2$



ফাংশন Domain (Case 3)

• $f(x) = \ln(2x - 3)$

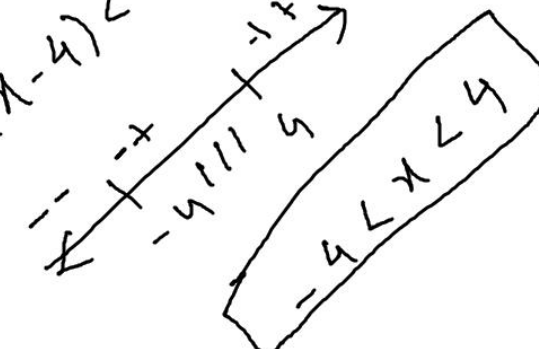
$2x - 3 > 0$
 $x > 3/2$

Things to Remember
 $\ln 3 = 1.09861..$
 $\ln 0 = \text{Math Error}$
 $\ln(-3) = \text{Math Error}$

• $f(x) = \log(16 - x^2)$

$f(x) = \ln$ [] > 0

$16 - x^2 > 0$
 $x^2 - 16 < 0$
 $(x+4)(x-4) < 0$



$-4 < x < 4$

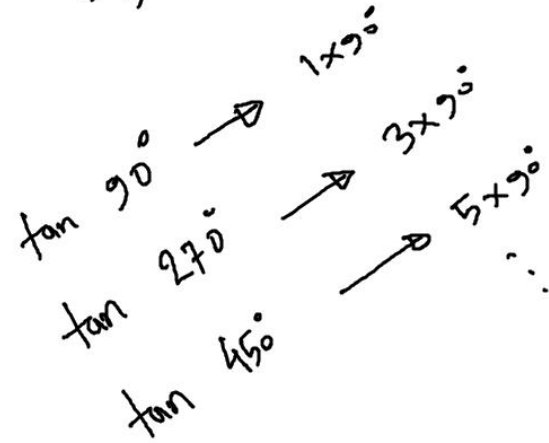


ফাংশন Domain (Case 3)

- $f(x) = \sin x$

- $f(x) = \tan x$

$D_f = \mathbb{R}$



$D_f = \mathbb{R} - \{90^\circ, 270^\circ, 450^\circ, \dots\}$
 $= \mathbb{R} - \left\{ (2n+1) \frac{\pi}{2} \right\}$



ফাংশন Domain (Poll Time – NDC Previous year)

Domain নির্ণয় করঃ $f(x) = \frac{\ln(2x-5)}{x-3}$

Option:

- A. $R - \left\{\frac{5}{2}\right\}$
- B. $R - \{3\}$
- C. $x \geq \frac{5}{2}$ and $x \neq 3$
- D. $x > \frac{5}{2}$ and $x \neq 3$

Handwritten notes and a boxed answer:

$2x - 5 > 0$
 $x > 5/2$

$x - 3 \neq 0$
 $x \neq 3$

and $x \neq 3$

$x > 5/2$ and $x \neq 3$



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ফাংশন Range

• $f(x) = \frac{2x}{3x-1}$

• $f(x) = \frac{5x-4}{2x+3}$

Range = $\mathbb{R} - \left\{ \frac{2}{3} \right\}$

Range = $\mathbb{R} - \left\{ \frac{5}{2} \right\}$

$f(x) = \frac{5}{3x+1}$

Range = $\mathbb{R} - \left\{ \frac{0}{3} \right\}$

= $\mathbb{R} - \{0\}$



ফাংশন Range

• $f(x) = x^2 + 4$



Range ≥ 4

• $f(x) = x^3 - 5$

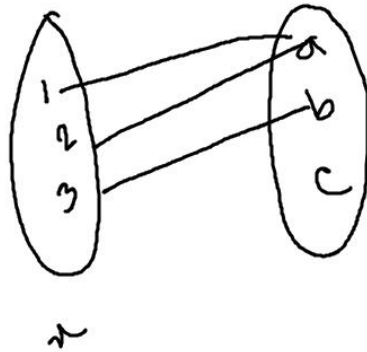


Range = \mathbb{R}

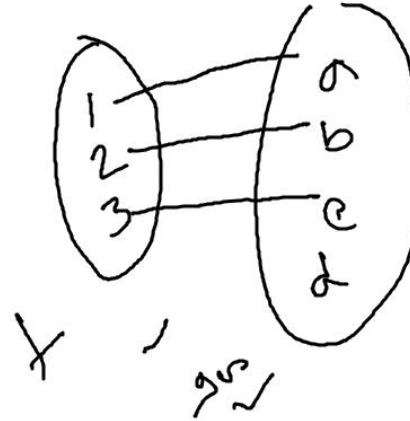
-8 - 5
-13

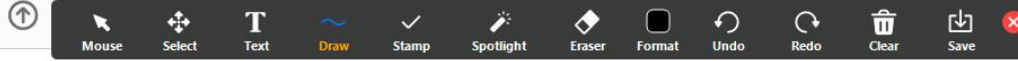


One to One Function (এক-এক ফাংশন)



~~সুচন x~~





Inverse Function (বিপরীত ফাংশন)

ধর, ছোট একটি বাচ্চা।



গেঞ্জি পড়ানো হল

শার্ট পড়ানো হল।

এখন বাচ্চাটিকে গোসল করানোর জন্যে তার প্রথমে

(i) শার্ট খুলতে হবে। then,

(ii) গেঞ্জি খুলতে হবে।

এখন লক্ষ্য কর,

$f(x) = 3x + 5$, যেখানে x হল ছোট বাচ্চা যার সাথে প্রথমে

3 গুণ করা হয়েছে তারপর 5 যোগ করা হয়েছে। এখন

বিপরীত ফাংশন বের করতে হলে প্রথমে 5 কে বিয়োগ

করতে হবে then 3 দ্বারা ভাগ করতে হবে।

অর্থাৎ, $f(x) = 3x + 5$,

$$\therefore f^{-1}(x) = \frac{x-5}{3}$$

$$\begin{array}{l} + 5 \\ \times 3 \\ \div 3 \end{array}$$

যা করা আছে, $\times 3, +5$,
যা করতে হবে, $-5, \div 3$



Inverse Function (বিপরীত ফাংশন)

- $f(x) = \frac{x^2+5}{3}$

$$f^{-1}(x) = \sqrt{3x-5}$$

- $f(x) = \left(\frac{3x^2+5}{4}\right)^{\frac{1}{3}}$

$$f^{-1}(x) = \left(\frac{4x^3-5}{3}\right)^{\frac{1}{2}}$$

$()^2 \times 5 \div 3$
 $+3$
 $()^2 \times 3 + 5 \div 4$
 $()^3 \times 4 - 5 \div 3$

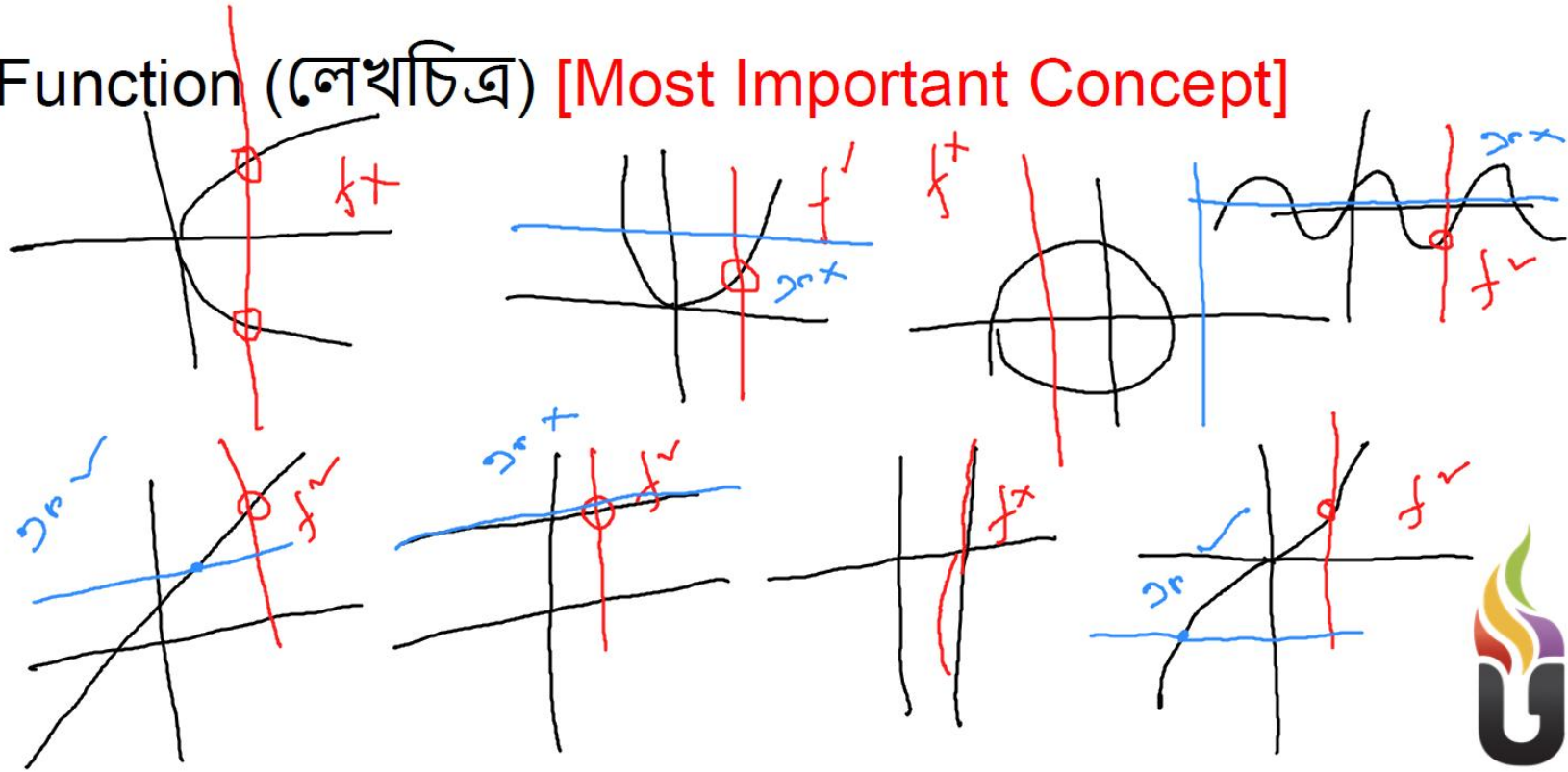
যা করা আছে $()^2, +5, \div 3$
 যা করতে হবে,
 $\times 3, -5, \sqrt{()}$

যা করা আছে,
 $()^2, \times 3, +5, \div 4, ()^{\frac{1}{3}}$
 যা করতে হবে।
 $()^3, \times 4, -5, \div 3, ()^{\frac{1}{2}}$



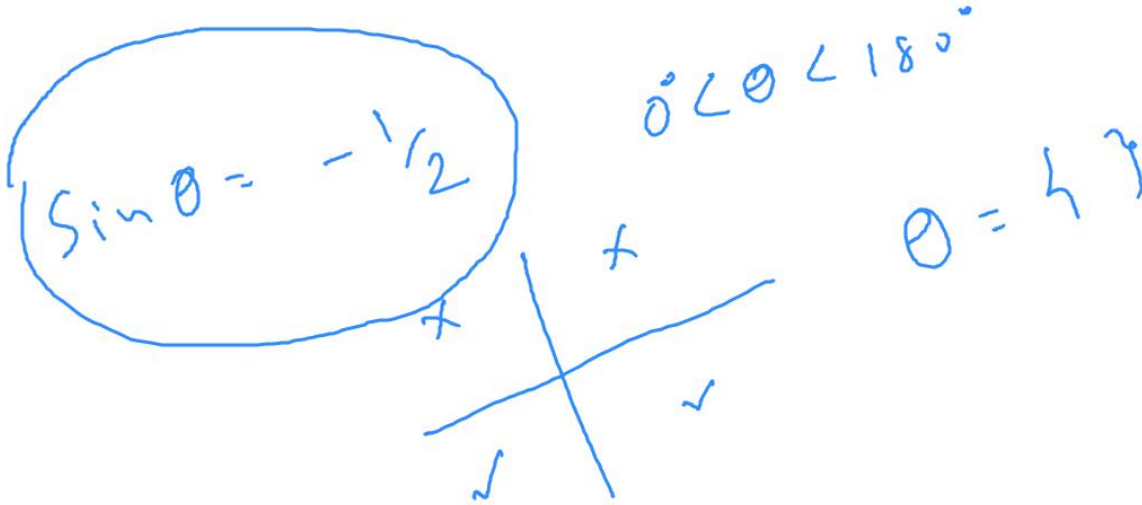
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Function (লেখচিত্র) [Most Important Concept]



ত্রিকোণমিতি [NDC Previous years]

$\sin \theta = \frac{1}{2}$; θ এর ৬ টি মান লিখো ?



Probability (Poll Time) [NDC Previous year]

3 টি মুদ্রা নিক্ষেপ করা হলে, কমপক্ষে 2 টি হেড আসার সম্ভাবনা কত?

Option:

- A. $\frac{1}{2}$
- B. $\frac{3}{8}$
- C. $\frac{1}{8}$
- D. $\frac{1}{8}$

Handwritten solutions showing the possible outcomes of 3 coin tosses:

H H H ✓	✓ T H H ✓
✓ H H T ✓	✓ T H T
✓ H T H ✓	✓ T T H
✓ H T T	✓ T T T

$\frac{7}{8}$

$$\frac{4}{8} = \frac{1}{2}$$



Any question

$$\frac{3x+2}{(x-1)(x+2)} = \frac{5/3}{x-1} + \frac{4/3}{x+2}$$

Partial fraction decomposition steps:

$$\frac{3x+2}{(x-1)(x+2)} = \frac{A}{x-1} + \frac{B}{x+2}$$
$$3x+2 = A(x+2) + B(x-1)$$
$$3x+2 = Ax + 2A + Bx - B$$
$$3x+2 = (A+B)x + (2A-B)$$
$$\begin{cases} A+B = 3 \\ 2A-B = 2 \end{cases}$$
$$\begin{matrix} 3x+2 \\ \underline{-(x+2)} \\ 2x \end{matrix} \Rightarrow \frac{2x}{2} = x$$
$$\begin{matrix} 3x+2 \\ \underline{-(x+2)} \\ 2x \\ \underline{-(2x-2)} \\ 4 \end{matrix} \Rightarrow \frac{4}{3}$$
$$\begin{matrix} 3x+2 \\ \underline{-(2x-2)} \\ x+4 \\ \underline{-(x+2)} \\ 2 \end{matrix} \Rightarrow \frac{2}{1}$$
$$\frac{5}{3} = \frac{5}{3}$$